

Class # 24 - Tues, Oct. 26

- Quiz # 3 - due Friday, Jan.
 - discuss at end of class.
- Midterm grades - next week.

- WebWork : 3 "Parabola" WW sets
 due Monday.

Today

- (1) Finish up "parabolas"
- (2) Distance formula
 ⇒ equations of circles.

(graphs of quadratic functions $y = ax^2 + bx + c$).

W

2

Review : graphs of quadratic polynomials

"parabolas"

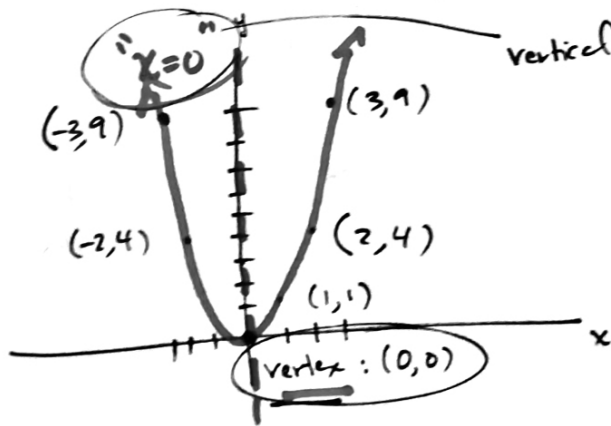
$$y = ax^2 + bx + c.$$

Ex : let's so back w look at the simplest, most basic quadratic polynomial.

$$y = x^2$$

What does the graph of "y = x²" look like?

x	y	(x, y)
0	$y = 0^2 = 0$	(0, 0)
1		(1, 1)
2		(2, 4)
3	$y = 3^2 = 9$	(3, 9)
-1		(-1, 1)
-2		(-2, 4)
-3	$y = (-3)^2 = 9$	(-3, 9)



vertical "axis of symmetry"

x-intercept: (0, 0)

y-intercept: (0, 0)

Paraboles: vertical and/or horizontal "shifts"

(3)

("Shifting Parabolas" - WebWork)

§9.7

"transformations"

"shift" basic parabola $y = x^2$

vertical shifts

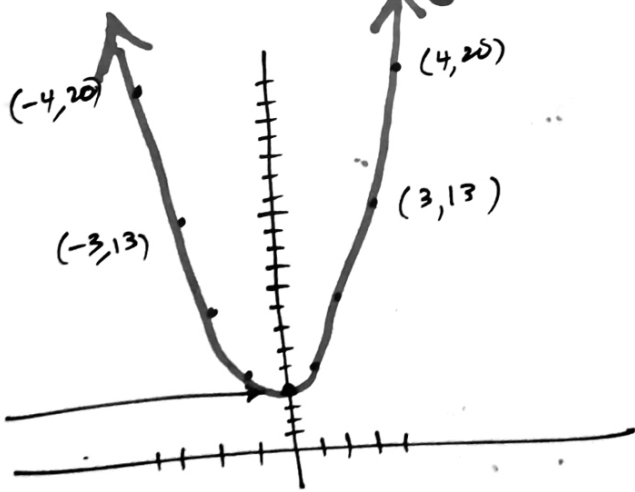
(1) $y = x^2 + k$

(where k is any constant #)

Table of (x,y) pts

OpenStax:
Example 9.53 / 9.54

Ex: Graph $y = x^2 + 4$



vertex?
(0, 4)

x	y = x ²	y = x ² + 4
0	0	4
±1	1	5
±2	4	8
±3	9	13
±4	16	20
±5	25	29
±6	36	40

(2) Horizontal shifts (of $y = x^2$)

\Rightarrow algebraically: $y = (x+h)^2$

$\Rightarrow y = (x-h)(x-h)$
 $= x^2 - xh - xh + h^2$
 $= \underline{\underline{x^2 - 2xh + h^2}}$

horizontal shift by h units.

very different from $y = x^2 + k$

Ex: (See OpenStax Ex 9.55/9.56)

- $y = (x-1)^2$: $y = x^2$ shifted right 1 unit
- $y = (x+1)^2$: $y = x^2$ shifted left 1 unit
- $y = (x-6)^2$

Ex: $y = (x-h)^2$ where $h < 0$

5

$h = -3 \Rightarrow$ horizontal shift left (of $y = x^2$)
by 3 units

$y = (x - (-3))^2$
 $y = (x + 3)^2$

