Mathematics 1375/D572, Spring 2019
Instructor: Suman Ganguli

Quiz \#2
Friday, February 8
$\qquad$

1. (6 points) Shown below is the graph of the function $f(x)=-x^{2}+4$ :

(a) Compute the following values of $f$ (show your calculations), and label the corresponding points on the graph above:

## Solution:

- $f(0)=-0^{2}+4=0+4=4$ (which means the point $(0,4)$ is on the graph)
- $f(1)=-\left(1^{2}\right)+4=-1+4=3$ (so the point $(1,3)$ is on the graph)
- $f(-3)=-\left(3^{2}\right)+4=-9+4=-5$ (so the point $(-3,-5)$ is on the graph)
(b) What is the domain of $f$ ? What is the range of $f$ ? For full credit, write the solutions in interval notation.


## Solution:

- The domain of $f$ is $\mathbb{R}$, i.e., all real numbers; in interval notation: $(-\infty, \infty)$
- Since the max value of $f(x)$ is $f(0)=4$ the range of $f$ is $(-\infty, 4]$

2. (4 points) Find the domain of each of the following functions. For full credit, write the solutions in interval notation.
(a)
$g(x)=\frac{1}{x-2}$

Solution: The domain consists of all real numbers except $x=2$, i.e., in interval notation: $(-\infty, 2) \cup(2, \infty)$
(b)

$$
h(x)=\sqrt{x+1}
$$

Solution: The domain consists of real numbers $x$ such that $x+1 \geq 0$, i.e., in $x \geq-1$. In interval notation: $[-1, \infty)$

