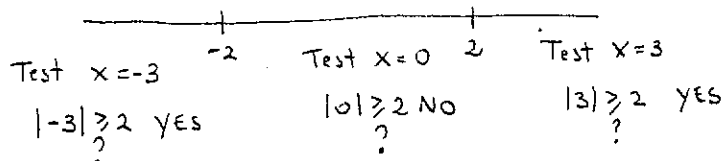


- ①  $(-\infty, -1)$
- ②  $(-5, \frac{1}{2}]$
- ③  $\sqrt{2}$
- ④  $0$
- ⑤  $\pi$
- ⑥  $f^{-1}(11) = 5$
- ⑦  $x = 8, -8$
- ⑧ No solution (the absolute value is never negative)
- ⑨  $(-\infty, -2] \cup [2, \infty)$

First solve  $|x|=2$  which gives  $x=2$  and  $x=-2$ . Then test a point in each interval.



⑩  $y = (x+3)^2 - 5$  (graph with Desmos to check!)

⑪ a)  $f(-1) = (-1)^2 - 2(-1) - 3 = 1 + 2 - 3 = \boxed{0}$

b)  $g(-4) = 2(-4) - 8 = \boxed{-16}$

c)  $f(x) = \boxed{x^2 - 2x - 3}$

d)  $f$  and  $g$  are both polynomials, so they both have domains  $\boxed{(-\infty, \infty)}$

e)  $(f+g)(5) = f(5) + g(5) = [25 - 10 - 3] + [10 - 8] = 12 + 2 = \boxed{14}$

[or:  $(f+g)(x) = x^2 - 11$  so  $(f+g)(5) = 25 - 11 = 14$ ]

f)  $\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)} = \boxed{\frac{x^2 - 2x - 3}{2x - 8}}$

g) We need  $2x - 8 \neq 0$  so  $x \neq 4$  domain  $\boxed{(-\infty, 4) \cup (4, \infty)}$

h)  $\left(\frac{g}{f}\right)(x) = \frac{g(x)}{f(x)} = \boxed{\frac{2x - 8}{x^2 - 2x - 3}}$

i) We need  $x^2 - 2x - 3 \neq 0$  Domain  $\boxed{(-\infty, -1) \cup (-1, 3) \cup (3, \infty)}$

$x^2 - 2x - 3 = 0$

$(x-3)(x+1) = 0$  gives  $x=3, x=-1$

j)  $(fg)(x) = f(x)g(x) = (x^2 - 2x - 3)(2x - 8) = 2x^3 - 8x^2 - 4x^2 + 16x - 6x + 24 = \boxed{2x^3 - 12x^2 + 10x + 24}$

k)  $(g \circ f)(2) = g(f(2)) = g(-3) = 2(-3) - 8 = \boxed{-14}$

$f(2) = 4 - 4 - 3 = -3$

l)  $(f \circ f)(0) = f(f(0)) = f(-3) = (-3)^2 - 2(-3) - 3 = 9 + 6 - 3 = \boxed{12}$

$$m) (f \circ g)(x) = f(g(x)) = f(2x-8) = (2x-8)^2 - 2(2x-8) - 3 =$$

$$4x^2 - 32x + 64 - 4x + 16 - 3 = \boxed{4x^2 - 36x + 77}$$

$$n) (g \circ f)(x) = g(f(x)) = 2(x^2 - 2x - 3) - 8 = \boxed{2x^2 - 4x - 14}$$

$$(12) \quad 3 - 5x \geq 0 \quad \frac{-5x \geq -3}{-5} \quad x \leq \frac{3}{5} \quad \boxed{(-\infty, \frac{3}{5}]}$$

$$(13) \quad |5x+4| = 11$$

$$\begin{array}{l} 5x+4 = 11 \\ 5x = 7 \quad x = \frac{7}{5} \end{array} \quad \left| \quad \begin{array}{l} 5x+4 = -11 \\ 5x = -15 \\ x = -3 \end{array} \right. \quad \boxed{\begin{array}{l} x = -3 \\ x = \frac{7}{5} \end{array}}$$

$$(14) \quad y = 9x - 3$$

$$x = 9y - 3 \quad (\text{switch } x \text{ and } y)$$

Solve for y:  $9y = x + 3$

$$\boxed{y = \frac{x+3}{9}}$$

(15) Make sure you bring the calculator to the exam!

This problem was shown in class

Zeros:  $x = -3.53, x = -2.35, x = -.12$

LOCAL MAXIMUM:  $(-3, 0)$

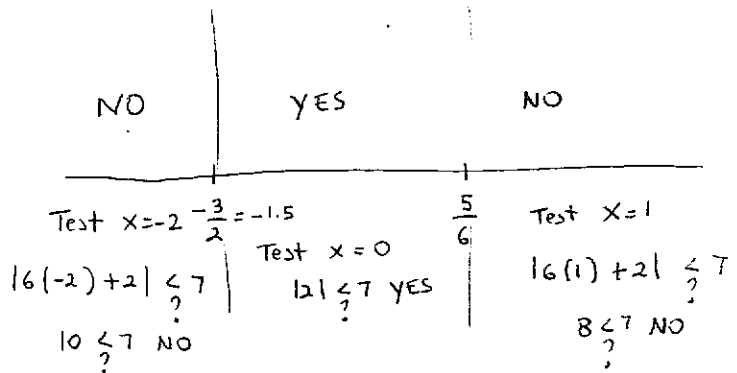
LOCAL MINIMUM:  $(-1, -3)$

$$(16) \quad |6x+2| < 7$$

$$|6x+2| = 7 \quad \text{gives} \quad x = -\frac{3}{2}, x = \frac{5}{6}$$

$$\begin{array}{l} 6x+2 = 7 \\ 6x = 5 \\ x = \frac{5}{6} \end{array} \quad \left| \quad \begin{array}{l} 6x+2 = -7 \\ 6x = -9 \\ x = -\frac{9}{6} = -\frac{3}{2} \end{array} \right.$$

$$\boxed{\left(-\frac{3}{2}, \frac{5}{6}\right)}$$



$$(17) \quad \frac{f(x+h) - f(x)}{h} = \frac{(x+h)^2 - 4(x+h) - 2 - (x^2 - 4x - 2)}{h} =$$

$$\frac{\cancel{x^2} + 2xh + h^2 - \cancel{4x} - 4h - \cancel{2} - \cancel{x^2} + \cancel{4x} + 2}{h} = \frac{h(2x+h-4)}{h} = \boxed{2x+h-4}$$