

## Linear Algebra Sections 1594

Pg.32

1) Compute  $\mathbf{u} + \mathbf{v}$  and  $\mathbf{u} - 2\mathbf{v}$ .

$$\mathbf{u} = \begin{bmatrix} -1 \\ 2 \end{bmatrix}, \mathbf{v} = \begin{bmatrix} -3 \\ -1 \end{bmatrix}$$

$$\begin{bmatrix} -1 \\ 2 \end{bmatrix} + \begin{bmatrix} -3 \\ -1 \end{bmatrix} = \begin{bmatrix} -4 \\ 1 \end{bmatrix} \qquad \begin{bmatrix} -1 \\ 2 \end{bmatrix} - 2 \begin{bmatrix} -3 \\ -1 \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \end{bmatrix} - \begin{bmatrix} -6 \\ -2 \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$$

11) Compute  $AD$  and  $DA$ . Explain how the columns or rows of  $A$  change when  $A$  is multiplied by  $D$  on the right or on the left. Find a  $3 \times 3$  matrix  $B$ , not the identity matrix or the zero matrix, such that  $AB = BA$ .

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} \text{ and } D = \begin{bmatrix} 5 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} \times \begin{bmatrix} 5 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 2 \end{bmatrix} = \begin{bmatrix} 1x5 + 2x0 + 3x0 & 1x0 + 2x3 + 3x0 & 1x0 + 2x0 + 3x2 \\ 2x5 + 4x0 + 5x0 & 2x0 + 4x3 + 5x0 & 2x0 + 4x0 + 5x2 \\ 3x5 + 5x0 + 6x0 & 3x0 + 5x3 + 6x0 & 3x0 + 5x0 + 6x2 \end{bmatrix}$$

**A****D****AD**

$$= \begin{bmatrix} 5 & 6 & 6 \\ 10 & 12 & 10 \\ 15 & 15 & 12 \end{bmatrix}$$

**AD**

$$\begin{bmatrix} 5 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 2 \end{bmatrix} \times \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} = \begin{bmatrix} 5x1 + 0x2 + 0x3 & 5x2 + 0x4 + 0x5 & 5x3 + 0x5 + 0x6 \\ 0x1 + 3x2 + 0x3 & 0x2 + 3x4 + 0x5 & 0x3 + 3x5 + 0x6 \\ 0x1 + 0x2 + 2x3 & 0x2 + 0x4 + 2x5 & 0x3 + 0x5 + 2x6 \end{bmatrix}$$

**D****A****DA**

$$= \begin{bmatrix} 5 & 10 & 15 \\ 6 & 12 & 15 \\ 6 & 10 & 12 \end{bmatrix}$$

**DA**

When  $A$  is multiplied by  $D$  we are multiplying the rows of  $A$  times the columns of  $D$ , and when  $D$  is multiplied by  $A$  we are multiplying the rows of  $D$  times the columns of  $A$ .

$$\begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} \times \begin{bmatrix} 5 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 5 \end{bmatrix} = \begin{bmatrix} 1x5 + 2x0 + 3x0 & 1x0 + 2x5 + 3x0 & 1x0 + 2x0 + 3x5 \\ 2x5 + 4x0 + 5x0 & 2x0 + 4x5 + 5x0 & 2x0 + 4x0 + 5x5 \\ 3x5 + 5x0 + 6x0 & 3x0 + 5x5 + 6x0 & 3x0 + 5x0 + 6x5 \end{bmatrix}$$

**A**

**B**

**AB**

$$= \begin{bmatrix} 5 & 10 & 15 \\ 10 & 20 & 25 \\ 15 & 25 & 30 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 5 \end{bmatrix} \times \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} = \begin{bmatrix} 5x1 + 0x2 + 0x3 & 5x2 + 0x4 + 0x5 & 5x3 + 0x5 + 0x6 \\ 0x1 + 5x2 + 0x3 & 0x2 + 5x4 + 0x5 & 0x3 + 5x5 + 0x6 \\ 0x1 + 0x2 + 5x3 & 0x2 + 0x4 + 5x5 & 0x3 + 0x5 + 5x6 \end{bmatrix}$$

**B**

**A**

**BA**

$$= \begin{bmatrix} 5 & 10 & 15 \\ 10 & 20 & 25 \\ 15 & 25 & 30 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 10 & 15 \\ 10 & 20 & 25 \\ 15 & 25 & 30 \end{bmatrix} = \begin{bmatrix} 5 & 10 & 15 \\ 10 & 20 & 25 \\ 15 & 25 & 30 \end{bmatrix}$$

$$\mathbf{AB} = \mathbf{BA}$$