

Group 1 Cumulative Practice Exam

1) Integration by Parts – Evaluate the indefinite integral:

$$\int 4x \cos(8x) dx$$

2) Trigonometric Substitution (*adjusted*) – Evaluate the indefinite integral:

$$\int \frac{2\sqrt{x^2 - 36}}{x^4} dx$$

3) Partial Fraction Decomposition – Evaluate the indefinite integral:

$$\int \frac{5x^2 - 10x + 8}{x(x - 2)^2} dx$$

4) Improper Integration (*adjusted*) – Determine whether the integral is divergent or convergent. If it is convergent, evaluate it. If it is divergent, answer “divergent”.

$$\int_{-5}^0 \frac{11}{\sqrt[7]{(x + 2)^9}} dx$$

5) Series Tests - Determine whether the following series converges or diverges. In your written work, state any convergence tests you used to determine your answer.

$$\sum_{n=1}^{\infty} \left(\frac{n + 3}{5n - 4} \right)^n$$

6) Alternating Series Test – Determine whether the following series converges absolutely, converges conditionally, or diverges. In your written work, state any convergence tests you used to determine your answer.

$$\sum_{n=1}^{\infty} (-1)^n \frac{1}{5n + 1}$$

7) Power Series - Find the center, radius of convergence and interval of convergence for the power series.

$$\sum_{n=0}^{\infty} \frac{(x - 2)^n}{n + 9}$$

8) Washers - Find the volume of the solid obtained by rotating the region bounded by the graphs of $y=13-x$, $y=2x+10$, $x=-5$ about the x -axis.

Practice Exam – Differentiation Options (Extra Practice)

Use only when students may need extra practice and have difficulties solving problems that would appear on the exam.

1) Evaluate the definite integral.

TOPIC: Antiderivatives (L1) and Definite Integrals (L2)

$$\int_1^4 8x^3 + 8x^7 - 20x^4 dx$$

2) Evaluate the indefinite integral.

TOPIC: Integration by Substitution (L3)

$$\int \frac{dx}{x - 60}$$

3) Evaluate the indefinite integral.

TOPIC: Integration by Parts (L4)

$$\int x * \sin(x) dx$$

4) Evaluate the indefinite integral using trig tables.

TOPIC: Integration Resulting in Inverse Trigonometric Functions

$$\int \frac{dx}{\sqrt{81 - x^2}}$$

5) Evaluate the indefinite integral.

TOPIC: Trigonometric Integrals (L5)

$$\int \sin^3(x) * \cos^4(x) dx$$

6) Evaluate the indefinite integral.

TOPIC: Trigonometric Substitution (L6)

$$\int \sqrt{x^2 + 25} dx$$

7) Evaluate the indefinite integral.

TOPIC: Partial Fraction Decomposition (L8)

$$\int \frac{5x - 1}{(x + 3)(x - 5)} dx = \frac{A}{x + 3} + \frac{B}{x - 5}$$

8) Determine whether the integral is divergent or convergent. If it is convergent, evaluate it. If it is divergent, answer "divergent."

TOPIC: Improper Integrals (L10)

$$\int_0^2 \frac{dx}{x^2}$$

9) Find the Maclaurin Polynomial of degree 4 for $f(x) = \sin(x)$, centered at $a = 0$.

TOPIC: Taylor and Maclaurin polynomials (L11)

10) If the following series converges, compute its sum. Otherwise, enter $+\infty$ if it diverges to infinity, $-\infty$ if it diverges to minus infinity, and DIV otherwise.

TOPIC: Infinite Series (L14)

$$\sum_{n=0}^{\infty} \frac{1}{n^{1.6}}$$

11) If the following series converges, compute its sum. Otherwise, enter $+\infty$ if it diverges to infinity, $-\infty$ if it diverges to minus infinity, and DIV otherwise.

TOPIC: Infinite Series (L14) – Alternating Series

$$\sum_{n=0}^{\infty} (-1)^n \frac{3n^2}{5n^2 - 6n}$$

12) If the following series converges, compute its sum. Otherwise, enter $+\infty$ if it diverges to infinity, $-\infty$ if it diverges to minus infinity, and DIV otherwise.

TOPIC: Infinite Series (L14) – Series Involving Exponentials and Factorials

$$\sum_{n=0}^{\infty} (-1)^n \frac{5^n}{2n!}$$

13) Compute the Riemann sum.

(1 point) The rectangles in the graph below illustrate a left endpoint Riemann sum for $f(x) = (15/x)$ on the interval $[2, 6]$.

The value of this left endpoint Riemann sum is , and this Riemann sum is

The graph shows the function $y = 15/x$ on the interval $[2, 6]$. The x-axis is labeled from 1 to 8, and the y-axis is labeled from 1 to 8. The function is a blue curve that decreases as x increases. The area under the curve from $x = 2$ to $x = 6$ is approximated by five blue rectangles. The left endpoint Riemann sum is used, so the height of each rectangle is determined by the function value at the left edge of the subinterval. The subintervals are $[2, 3]$, $[3, 4]$, $[4, 5]$, $[5, 6]$, and $[6, 6]$ (which has zero width). The heights of the rectangles are $15/2 = 7.5$, $15/3 = 5$, $15/4 = 3.75$, $15/5 = 3$, and $15/6 = 2.5$. The total area of the rectangles is $7.5 \times 1 + 5 \times 1 + 3.75 \times 1 + 3 \times 1 + 2.5 \times 1 = 22.75$.

Left endpoint Riemann sum for $y = (15/x)$ on $[2, 6]$

