

**MODULE 4****INVERSE FUNCTIONS  
AND LONG DIVISION**

Name: \_\_\_\_\_ Points: \_\_\_\_\_

**Exercise 1.** Find the inverse of the given function.

(a)  $f(x) = \frac{1}{x-5} + 5$

(b)  $f(x) = \frac{3x^2-7}{8-5x^2}, \quad \text{for } x \geq 0$

(c)  $f(x) = x^2 + 3, \quad \text{for } x \geq 0$

(d)  $f(x) = x^2 + 3, \quad \text{for } x \leq 0$

**Exercise 2.** Check if the functions are inverses of each other. If so, what are the domains and ranges where they are inverses?

(a)  $f(x) = \sqrt{x+6}$  and  $g(x) = (x-6)^2$

(b)  $f(x) = |x|$  and  $g(x) = x$

(c)  $f(x) = |x|$  and  $g(x) = -x$

**Exercise 3.** Divide using long division.

(a)  $(x^4 + 3x^3 - 2x^2 + 9x + 8) \div (x + 4) =$

(b)  $(6x^3 + 5x^2 - 14x - 10) \div (2x + 3) =$

**Exercise 4.**

(a) Check that 2 is a root of  $f(x) = x^5 - 4x^3 + 7x - 14$  and use this to factor  $f$ .

(b) Check that  $-3$  is a root of  $f(x) = x^3 + 8x^2 + 18x + 9$  and use this to factor  $f$ .