# NEW YORK CITY COLLEGE OF TECHNOLOGY The City University of New York 

DEPARTMENT:
COURSE:

TITLE:

DESCRIPTION:

TEXT:

CREDITS:

PREREQUISITES:

## Mathematics

MAT 2440

Discrete Structures and Algorithms I
This course introduces the foundations of discrete mathematics as they apply to computer science, focusing on providing a solid theoretical foundation for further work. Topics include functions, relations, sets, simple proof techniques, Boolean algebra, propositional logic, elementary number theory, writing, analyzing and testing algorithms.

Discrete Mathematics and Its Applications, $8^{\text {th }}$ edition by Kenneth H. Rosen
McGraw-Hill

3 (2 class hours, 2 lab hours)
MAT 1375 or higher and one of the following: CST 1201 or CST 2403 or MAT 1630

Prepared by Professors Henry Africk, Brad Isaacson, Caner Koca, Nan Li, Satyanand Singh, Arnavaz Taraporevala, Johann Thiel. (Fall 2017)
Revised by Professors Arnavaz Taraporevala, Johann Thiel (Spring 2020)
A. Testing Guidelines:

The following exams should be scheduled:

1. A one-hour exam at the end of the First Quarter
2. A one-session exam at the end of the Second Quarter
3. A one-hour exam at the end of the Third Quarter
4. A one-session Final Examination
B. A Computer Algebra System will be used in class and for a project.

## Course Intended Learning Outcomes/Assessment Methods

| Learning Outcomes | Assessment Methods |
| :--- | :--- |
| 1. Use the rules of logic to understand mathematical <br> statements and prove propositions using <br> - A direct proof <br> - An indirect proof <br> - A proof by contradiction <br> - A proof by induction | Classroom activities and discussion, <br> homework, project, exams. |
| 2. Write simple algorithms using pseudocode and <br> understand the efficiency of algorithms. | Classroom activities and discussion, <br> homework, project, exams. |
| 3. Understand basic number theory topics. | Classroom activities and discussion, <br> homework, project, exams. |
| 4. Use computer technology to assist in the above. | Classroom activities and discussion, <br> homework, project, exams. |

## General Education Learning Outcomes/Assessment Methods

| Learning Outcomes | Assessment Methods |
| :--- | :--- |
| 1. Gather, interpret, evaluate, and apply information <br> discerningly from a variety of sources. | Classroom activities and discussion, <br> homework, project, exams. |
| 2. Understand and employ both quantitative and <br> qualitative analysis to solve problems. | Classroom activities and discussion, <br> homework, project, exams. |
| 3. Employ scientific reasoning and logical thinking. | Classroom activities and discussion, <br> homework, project, exams. |
| 4. Communicate effectively using written and oral <br> means. | Classroom activities and discussion, <br> homework, project, exams. |
| 5. Utilize computer based technology in accessing <br> information, solving problems and communicating. | Classroom activities and discussion, <br> homework, project, exams. |
| 6. Work with teams. Build consensus and use <br> creativity. | Classroom activities and discussion, <br> project, homework. |
| 7. Acquire tools for lifelong learning. | Classroom activities and discussion, <br> homework, project, exams. |

## New York City College of Technology Policy on Academic Integrity

Students and all others who work with information, ideas, texts, images, music, inventions, and other intellectual property owe their audience and sources accuracy and honesty in using, crediting, and citing sources. As a community of intellectual and professional workers, the College recognizes its responsibility for providing instruction in information literacy and academic integrity, offering models of good practice, and responding vigilantly and appropriately to infractions of academic integrity. Accordingly, academic dishonesty is prohibited in The City University of New York and at New York City College of Technology and is punishable by penalties, including failing grades, suspension, and expulsion. The complete text of the College policy on Academic Integrity may be found in the catalog.

## Writing Intensive Course Designation

This course has been designated as a "Writing Intensive" (WI) course by City Tech. A WI course includes critical reading, logical thinking, and the use of writing to help students understand the topic; the use of appropriate style and disciplinary conventions in writing and speaking; the use of research resources, including the library, specific to the discipline; a detailed syllabus; a comprehensive course calendar; and a minimum of fifteen pages of writing per student. Writing assignments will be both formal (graded) and informal (nongraded).

Written work will be a mandatory part of the course. This can include coding projects, proofs, and written assignments. Written work will account for a minimum of $10 \%$ of the overall grade in the course.

| Lec. | Discrete Structures and Algorithms I | Homework |
| :---: | :--- | :--- |
| 1 | 1.1 Propositional Logic (1-13) | (P. 13) 1, 3, 11, 13, 25, 29, 31, 33, 39, 48 |
| 2 | 1.2 Applications of Propositional Logic (17-23) | (P. 23) 1-3, 7, 44, 45 |
| 3 | 1.3 Propositional Equivalences (26-37) | (P. 38) 3, 4, 6, 7, 8, 11, 27 |
| 4 | 1.4 Predicates and Quantifiers (40-56) | (P. 56) 1, 2, 4, 7-13 odd, 19, 30, 38 <br> (P. 68) 1, 3, 10, 27, 31, 33 |
| 1.5 Nested Quantifiers (60-68) | (P. 82) 5, 6, 19, 20, 35 |  |
| 5 | 1.6 Rules of Inference (73-82) | (P. 95) 1-4, 9-12, 19, 20 |
| 6 | 1.7 Introduction to Proofs (84-95) | (P. 131) 1, 7, 13, 21 (a)\& (b), 29, 30, 33, 37 |
| 7 | Test 1 | (P. 136) 3, 15(b), 19(b), 23-25, 28, 52, 53, 58-60 |
| 8 | 2.1 Sets (121-131) | (P. 161) 3, 9-12, 15, 20, 23, 30, 33, 41, 44-46, 60-63 |
| 9 | 2.2 Set Operations (133-144) | (P. 177) 3, 9, 25, 29-31, 33, 35, 45 |
| 10 | 2.3 Functions (147-161) | (P. 186) 1, 3, 11 |
| 11 | 2.4 Sequences and Summations (163-177) | (P. 213) 1, 3-15 odd, 16-18, 36, 37, 39-41, 56, 57 |
| 12 | 2.5 Cardinality of Sets (179-186) (optional) |  |
| $13-15$ | 3.1 Algorithms (201-213) | (P. 228) 1-27 odd, 34-42 |
| 16 | Test 2 | (P. 241) 1-5, 20, 22, 40 |
| $17-18$ | 3.2 The Growth of Functions (216-228) | (P. 258) 1, 13, 21, 27, 31-35, 36, 47 |
| $19-21$ | 3.3 Complexity of Algorithms (231-241) | (P. 269) 1-15 odd, 57, 58 <br> (P. 288) 1, 3, 17, 25, 27, 33 |
| 22 | 4.1 Divisibility and Modular Arithmetic (251-258) | (P. 301) 1, 5, 11, 21, 33, 34, 55 <br> (P. 308) 1-5 odd |
| 23 | 4.2 Integer Representations and Algorithms (260-268) <br> 4.3 Primes and Greatest Common Divisors (271-288) |  |
| 24 | 4.4 Solving Congruences (290-300) <br> 4.5 Applications of Congruences (303-308) | (P. 322) 1-5 odd |
| 25 | 4.6 Cryptography (310-321) |  |
| 26 | Test 3 | (P. 350) 1-11 odd, 15, 21 |
| $27-28$ | 5.1 Mathematical Induction (331-350) | (P. 398) 3,7 |
| 28 | 5.5 Program Correctness (393-398) (optional) |  |
| 29 | Review |  |
| 30 | Final Exam |  |


| Lec. | Discrete Structures and Algorithms I | Homework |
| :---: | :--- | :--- |
| 1 | 1.1 Propositional Logic (1-12) | (P. 12) 1, 3, 9, 11, 23, 27, 29, 31, 37, 44 |
| 2 | 1.2 Applications of Propositional Logic (16-22) | (P. 22) 1-3, 7, 40, 41 |
| 3 | 1.3 Propositional Equivalences (25-34) | (P. 34) 3, 4, 6, 7, 8, 9, 23 |
| 4 | 1.4 Predicates and Quantifiers (36-52) | (P. 53) 1, 2, 4, 7-13 odd, 19, 30, 36 <br> (P. 64) 1, 3, 10, 27, 31, 33 |
| 1.5 Nested Quantifiers (57-64) | (P. 79) 5, 6, 19, 20, 35 |  |
| 5 | 1.6 Rules of Inference (69-78) | (P. 91) 1-4, 9-12, 17, 18 |
| 6 | 1.7 Introduction to Proofs (80-90) | (P. 125) 1, 5, 11, 19(a)\&(b), 27, 28, 31, 35 |
| 7 | Test 1 | (P. 136) 3, 15(b), 17(b), 21-23, 26, 46, 47, 52-55 |
| 8 | 2.1 Sets (115-125) | (P. 152) 3, 9, 10-12, 15, 20, 23, 30, 33, 39, 42-44, 58-61 |
| 9 | 2.2 Set Operations (127-135) | (P. 167) 3, 9, 25, 29, 30, 31, 33, 35, 43 |
| 10 | 2.3 Functions (138-152) | (P. 176) 1, 3, 11 |
| 11 | 2.4 Sequences and Summations (156-167) | (P. 202) 1, 3-15 odd, 16-18, 34, 35, 37-39, 52, 53 |
| 12 | 2.5 Cardinality of Sets (170-176) (optional) |  |
| $13-15$ | 3.1 Algorithms (191-202) | (P. 216) 1-27 odd, 34-42 |
| 16 | Test 2 | (P. 229) 1-5, 20, 22, 36 |
| $17-18$ | 3.2 The Growth of Functions (204-216) | (P. 244) 1, 9, 15, 21, 26-29, 30, 21 |
| $19-21$ | 3.3 Complexity of Algorithms (218-229) | (P. 255) 1-15 odd, 51, 52 <br> (P. 272) 1, 3, 17, 25, 27, 33 |
| 22 | 4.1 Divisibility and Modular Arithmetic (23-244) | (P. 284) 1, 5, 11, 21, 33, 34, 55 <br> (P. 292) 1-5 odd |
| 23 | 4.2 Integer Representations and Algorithms (245-254) <br> 4.3 Primes and Greatest Common Divisors (257-272) |  |
| 24 | 4.4 Solving Congruences (274-284) <br> 4.5 Applications of Congruences (287-292) | (P. 304) 1-5 odd |
| 25 | 4.6 Cryptography (294-303) |  |
| 26 | Test 3 | (P. 329) 1-11 odd, 15, 21 |
| $27-28$ | 5.1 Mathematical Induction (311-329) | (P. 377) 3,7 |
| 28 | 5.5 Program Correctness (372-376) (optional) |  |
| 29 | Review |  |
| 30 | Final Exam |  |

## List of Suggested Projects

1. Lecture 13 \& 14: Implement the max and linear search algorithms in a programming language.
2. Lecture 21: Timing algorithms by input size.
3. Lecture 23: Primality testing using a programming language.
4. Lecture 24: Implement a hashing function and a pseudorandom generator in a programming language.
5. Lecture 25: Implement a Caesar cipher.
6. Lecture 27: Implement a Tower of Hanoi game.
