## CITY UNIVERSITY OF NEW YORK - NEW YORK CITY COLLEGE OF TECHNOLOGY

# MAT 2675 - SPRING 2019 EXPERIMENTAL COURSE OUTLINE 

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## TEXTBOOKS

The proposed outline uses two Open Educational Resource (OER) textbooks.

1. Whitman Calculus (Chapters 12-16),
a. available to browse at this link https://www.whitman.edu/mathematics/calculus online/ with interactive images
b. available to download at https://www.whitman.edu/mathematics/multivariable/multivariable.pdf
2. OpenStax Calculus 3 (Chapters 1-6)
a. available to browse at https://cnx.org/contents/oxzXkyFi@3.7:Zh8bDwa-@16/Preface
b. available to download at https://cnx.org/exports/a31cd793-2162-4ege-acb5-

6e6bbd76a5fa@3.7.pdf/calculus-volume-3-3.7.pdf
Whitman Calculus will be the required text, and OpenStax Calculus 3 will be used as a supplementary/optional resource.

## WEBWORK

In Fall 2015, I had compiled problem sets on WeBWork based on our current MAT2675 outline. I will continue using it for the proposed experimental outline with only minor adjustments. Whitman Calculus provides a compilation of WeBWork questions available at https://www.whitman.edu/mathematics/webwork/Guichard-Calc3-Webwork20121209.tgz.

PROPOSED EXPERIMENTAL OUTLINE \& COMPARISON WITH THE CURRENT OUTLINE

| Lec. | Topics in Current Outline | Topics in the Proposed <br> Outline | Reading <br> (Whitman) | Reading <br> (Openstax) |
| :--- | :--- | :--- | :--- | :--- |
|  | 9.1 Vectors in the Plane <br> 9.2 Vectors in Three-dimensional <br> Space | Points in space. <br> Coordinate Systems | 12.1 | 2.7 |
|  | 9.3 The Dot Product and Applications <br> (P. 741-745) | Vectors in space <br> Dot Product | 12.6 |  |
|  | 9.4 The Cross Product (P. 753-759) | Cross Product | 12.2 | 2.1 |
| 3 | $\mathbf{9 . 5}$ Lines and Planes in Space | Lines and Planes in Space | 12.2 | 2.3 |


| 4 | 10.1 Vector-Valued Functions -Limits, Derivatives and Continuity 10.2 Velocity (P. 805-807) | Vector valued functions and space curves Tangent vectors to curves | $\begin{aligned} & 13.1 \\ & 13.2 \\ & 13.3 \end{aligned}$ | $\begin{aligned} & 3.1 \\ & 3.2 \\ & 3.3 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| 5 | 10.3 Tangent Vectors and Arc Length (P. 813-820) | Multivariable functions Quadric Surfaces | $\begin{aligned} & 14.1 \\ & 14.2 \end{aligned}$ | $\begin{aligned} & 4.1 \\ & 2.6 \end{aligned}$ |
| 6 | 11.1 Functions of Several Variables | Partial Derivatives Tangent Planes | $\begin{aligned} & 14.3 \\ & 14.6 \\ & \hline \end{aligned}$ | $\begin{aligned} & 4.3 \\ & 4.4 \end{aligned}$ |
| 7 | 11.3 Limits and Continuity | Chain Rule | 14.4 | 4.5 |
| 8 | First Examination | Test 1 |  |  |
| 9 | 11.4 Partial Derivatives | Directional Derivatives Gradient | 14.5 | 4.6 |
| 10 | 11.5 Differentiability and the Chain Rule | Max-Min Problems | 14.7 | 4.7 |
| 11 | 11.6 Gradients and Directional Derivatives | Lagrange Multipliers | 14.8 | 4.8 |
| 12 | 11.7 Tangent Planes | Volume under graphs | 15.1 | 5.1 |
| 13 | 11.8 Maximum-Minimum Problems | Double and iterated integrals | 15.1 | 5.2 |
| 14 | 11.9 Lagrange Multipliers | Double integral in polar coordinates | 15.2 | $5 \cdot 3$ |
| 15 | 12.1 Double Integrals Over Rectangular Regions | Review |  |  |
| 16 | Second Examination | Test 2 |  |  |
| 17 | 12.2 Integration Over More General Regions | Triple integrals | 15.5 | 5.4 |
| 18 | 12.3 Calculation of Volumes of Solids | Double integrals in spherical and cylindrical coordinates | 15.6 | 5.5 |
| 19 | 12.4 Polar Coordinates | Change of Variables and jacobians | 15.7 | 5.7 |
| 20 | 12.5 Integrating in Polar Coordinates | Vector fields Line integrals | $\begin{aligned} & 16.1 \\ & 16.2 \end{aligned}$ | $\begin{aligned} & 6.1 \\ & 6,2 \end{aligned}$ |
| 21 | 12.6 Triple Integrals | Conservative vector fields | 16.3 | 6.3 |
| 22 | 13.1 Vector Fields | Green's Theorem | 16.4 | 6.4 |
| 23 | 13.2 Line Integrals | Divergence and Curl | 16.5 | 6.5 |
| 24 | Third Examination | Test 3 |  |  |
| 25 | 13.3 Conservative Vector Fields and Path Independence | Vector functions on surfaces Surface integrals Surface area | $\begin{aligned} & 16.6 \\ & 16.7 \\ & 15.4 \\ & \hline \end{aligned}$ | 6.6 |
| 26 | 13.4 Divergence, Gradient, and Curl | Stokes' Theorem | 16.8 | 6.7 |


| 27 | 13.5 Green's Theorem | Stokes' Theorem,ctd <br> Gauss' Theorem | 16.8 <br> 6.9 | 6.7 <br> 6.8 |
| :--- | :--- | :--- | :--- | :--- |
| 28 | 13.6 Surface Integrals | Gauss' Theorem, ctd | 16.9 | 6.8 |
| 29 | Review | Review |  |  |
| 30 | Final Examination | Final |  |  |

## MAIN DIFFERENCES WITH THE CURRENT OUTLINE

The new outline allocates less time on "theoretical" topics such as limits, continuity, and differentiability of multivariable functions, with the aim of covering Gauss Theorem and Stokes Theorem in depth at the end of the semester. The pace of the course will be slightly faster in the beginning, up until Test 1.

