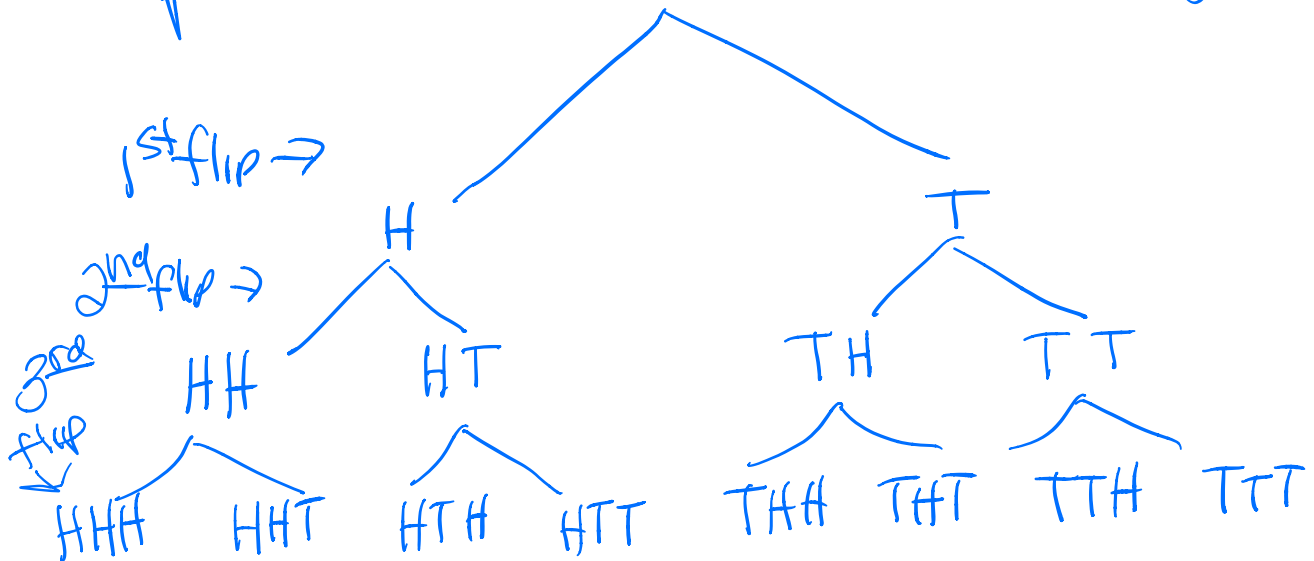


# Word doc Lecture #6

## Examples

4) Flip a coin 3 times. Want to list all possible outcomes. Create a tree diagram.



a) So the sample space for this experiment

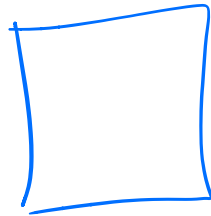
is  $S = \{ \underline{HHH}, \underline{HHT}, \underline{HTH}, \underline{HTT}, \underline{THH}, \underline{THT}, \underline{TTH}, \underline{TTT} \}$  (8 outcomes)

b) Event that tails occur more often than heads?

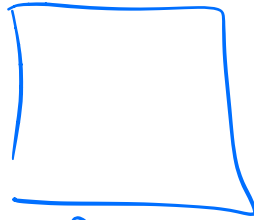
$A = \{ HTT, THT, TTH, TTT \}$

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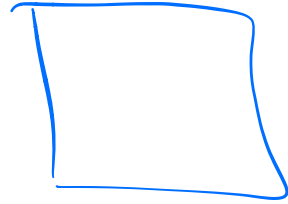
## Probability Example :



Door 1



Door 2



Door 3

Behind one door is a car

Behind the others are goats.

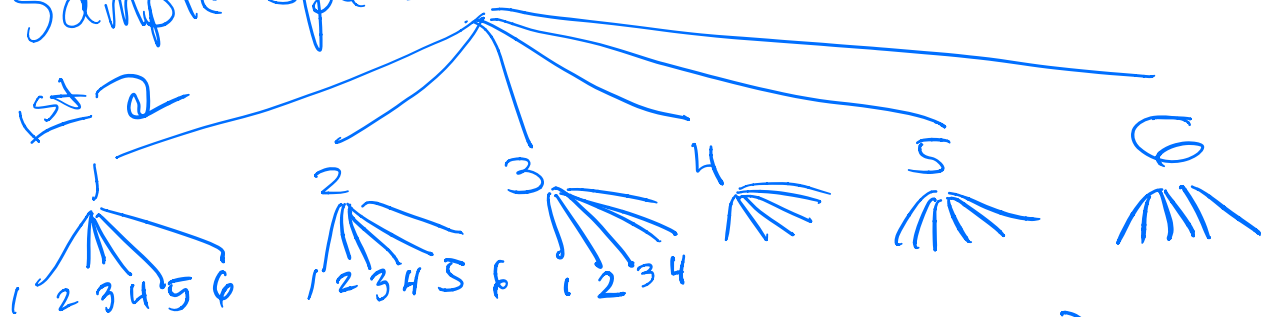
Monty asks you to choose a door. Monty then reveals what is behind one of the other doors. Monty now asks

you: Do you want to stay with your original choice or switch?

---

5) Roll 2 dice:

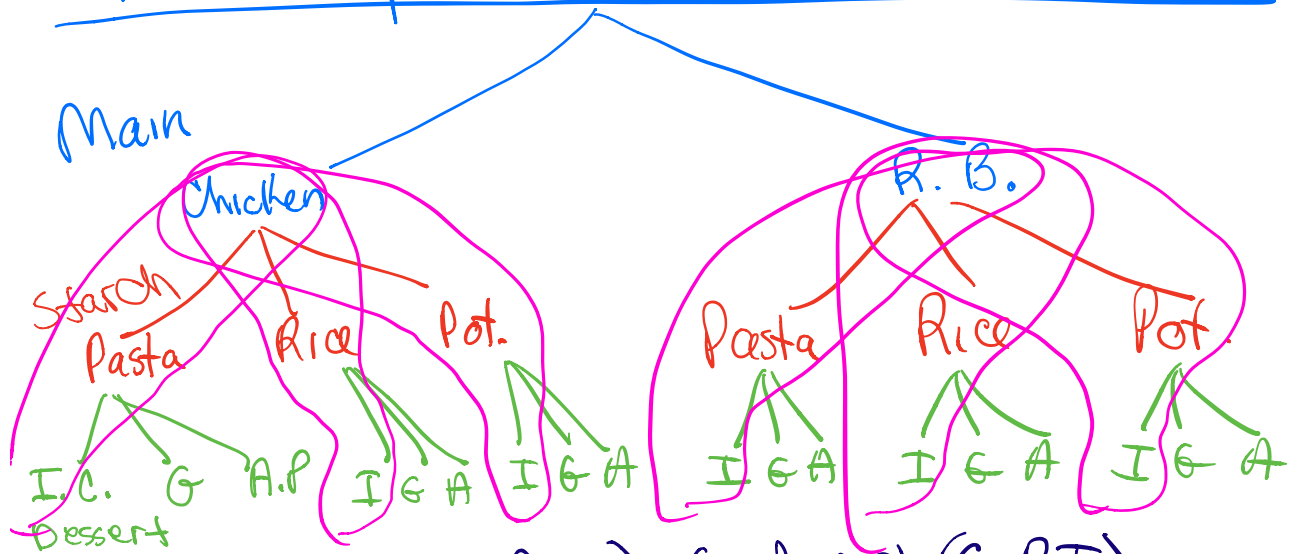
Sample Space:



$S = \{(1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (2,1), \dots\}$

You solve parts b) + c)!

Main



$S = \{(Ch, Pas, I), (C, Pas, G), (C, P, A.P), (C, R, I), \dots, (R.B, Pot, A)\}$

a)  $2 \times 3 \times 3 = 18$  outcomes

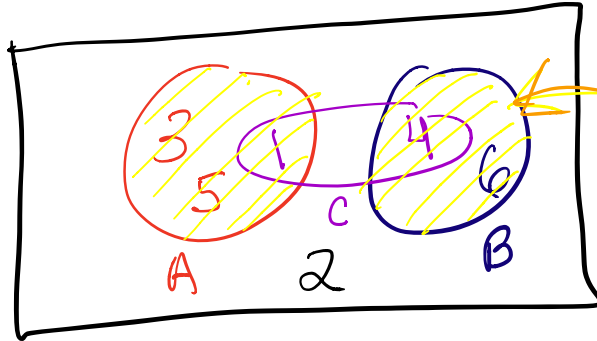
b) A = ice cream is chosen =  $\{(Chick, Pasta, I.C.), (Chicken, Rice, I.C.), (Ch, Pot, I.C.), (R.B, Pasta, I.C.) (R.B, Rice, I.C.) (R.B, Pot., I.C.)\}$

# Venn Diagrams:

Ex  $S = \{1, 2, 3, 4, 5, 6\}$ ,  $A = \{1, 3, 5\}$ ,  $B = \{4, 6\}$ ,  $C = \{1, 4\}$

Find  
a)  $A \cup B = \{1, 3, 4, 5, 6\}$

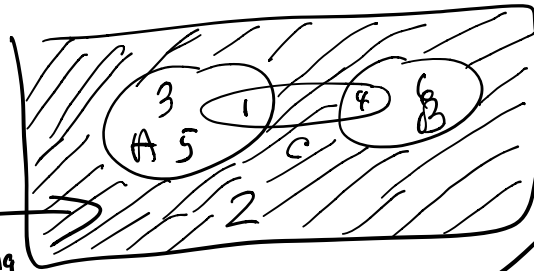
↑  
"union"  
You do "or"  
b) + c)! Have fun!



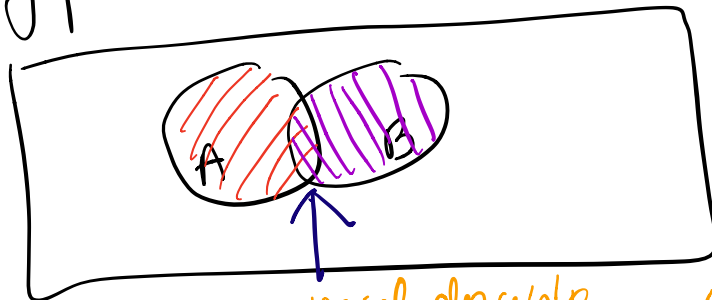
union

d)  $(A \cup B)^c$   
 $= \{2\}$

complement  
shade everything  
outside of yellow  $(A \cup B)$



# Counting principles:



avoid double counting!!

For any sets  
 $A + B$ :

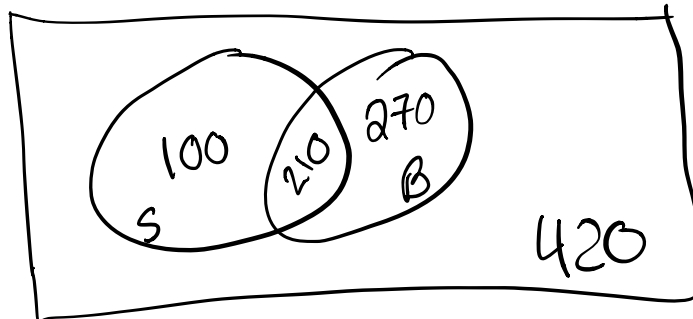
$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

↑  
intersection

If  $A + B$  are disjoint  $\rightarrow$  no worries

$$n(A \cup B) = n(A) + n(B)$$

Ex Survey 1000 people  
 310 stocks = S  
 480 bonds = B  
 210 stocks + bonds



$$1000 - (100 + 210 + 270)$$

$$= 1000 - 580$$

$$= 420$$

a) How many invested in S or B? =  $100 + 210 + 270$   
 = 580  
 "or" → "union"

b) neither stocks nor bonds = saying "not or"  
 $\neg (S \cup B)$  also say  $(S \cup B)^c$   
 "not" → complement = 420

c) Bonds but not stocks? 270