

2/8/2022

GCF + Factoring by Grouping (continued)

Recall: The GCF of a list of common variables raised to powers is the variable raised to the **smallest exponent** in the list.

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WebWork Set: GCF Grouping

#2)  $10x^5 + 35x^4$  (Factor)

Find the GCF

$$\text{Factor: } 10x^5 = 2 \cdot 5 \cdot x^5$$

$$\text{Factor: } 35x^4 = 5 \cdot 7 \cdot x^4$$

$$\text{GCF} = 5x^4 \quad \text{Now use this}$$

to factor:  $\boxed{5x^4(2x + 7)}$

WW #5)

$$4x(y+8) - 3(y+8)$$

GCF:  $y+8$   
factor  
→

$$4x(y+8) - 3(y+8) = (y+8)(4x - 3)$$

← multiply

WW #6) Factor

$$49AB + 28A + 14B + 8$$

$$\rightarrow 7^2AB + 2^2 \cdot 7A + 2 \cdot 7B + 2^3$$

Try first to find a GCF for all terms appearing. In this case, there are no common terms for all.

Instead group terms together and factor the groups

$$(7^2 AB + 2^2 \cdot 7A) + (2 \cdot 7B + 2^3)$$

$$7A(7B + 2^2) + 2(7B + 2^2)$$

$$= (7B + 2^2)(7A + 2)$$

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## Class Agenda 6

use what we learned to factor polynomials with 3 terms i.e. trinomials

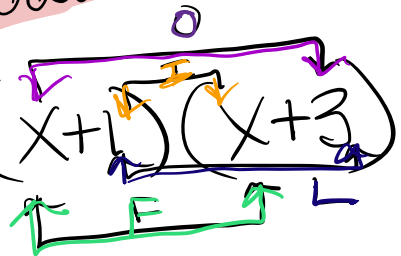
Recall: <sup>EX</sup> Factor

$$x^2 + 4x + 3$$

Sum

$$= (x+1)(x+3)$$

product



"FOIL"  
↑    ↑    ↑    ← last  
outer inner  
first

Now, what if the leading term has a coefficient other than 1?!

Ex  $2x^2 + 11x + 12$

product  $2 \cdot 12 = 24$

product, multiply to 24 : 8, 3  
and sum to 11 : 8, 3

Now what do we do with these numbers?! Swap out  $11x$  for  $8x + 3x$

$$2x^2 + 11x + 12$$
$$= 2x^2 + 8x + 3x + 12$$

Now factor by grouping!

$$= (2x^2 + 8x) + (3x + 12)$$

$$= 2x(x+4) + 3(x+4)$$

$$= (x+4)(2x+3)$$

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Recall: If our polynomial has 2 terms (i.e. is a binomial) and it looks like the difference of two perfect squares we have a formula for factoring:

$$a^2 - b^2 = (a+b)(a-b)$$

WW set difference of two squares

#1)

$$x^2 - 16$$
$$= x^2 - 4^2 = (x+4)(x-4)$$

Ex

$$36x^2 - 24y^2$$
$$= (6x)^2 - (2y)^2 = (6x+2y)(6x-2y)$$

$$49a^4 - 81b^{16}$$
$$= (7a^2)^2 - (9b^8)^2$$
$$= (7a^2 - 9b^8)(7a^2 + 9b^8)$$