

$$\begin{aligned}
 (1) & 4x + 5y + 12z = 5 && \text{WW set} \\
 (2) & -x + 4y + 8z = -14 && \text{3x3 systems} \\
 (3) & -3x + y - 20z = -31 && \neq 4
 \end{aligned}$$

Choose (1) + (2) + Kill x!

$$\begin{array}{r|l}
 (1) & 4x + 5y + 12z = 5 \\
 (2) & -x + 4y + 8z = -14 \\
 \hline
 (1) & 4x + 5y + 12z = 5 & -14 \\
 & & \times 4 \\
 & & \hline
 & & -56 \\
 (4) = 4(2) & -4x + 16y + 32z = -56 \\
 \hline
 (5) = (1) + (4) & 21y + 44z = -51 \quad \neq
 \end{array}$$

Now choose (2) + (3) MUST KILL
The same variable! X!

$$\begin{array}{r|l}
 (2) & -x + 4y + 8z = -14 \\
 (3) & -3x + y - 20z = -31 \\
 \hline
 (6) = -3(2) & 3x - 12y - 24z = +42 \\
 (3) & -3x + y - 20z = -31
 \end{array}$$

$$\begin{array}{r} -14 \\ x - 3 \\ \hline +42 \end{array}$$

$$(7) = (6) + (3) \quad \left| \quad * -11y - 44z = +11 \right.$$

Now solve the new system,
2 equations, only 2 variables

$$\begin{array}{l} (5) \quad 21y + 44z = -51 \\ (7) \quad -11y - 44z = 11 \end{array}$$

$$(8) \quad (5) + (7) \quad 10y = -40$$

$$y = -4$$

Now substitute (10) into

$$(5) \quad 21(-4) + 44z = -51$$

$$\begin{array}{r} -84 + 44z = -51 \\ +84 \qquad +84 \end{array}$$

$$\begin{array}{r} 84 \\ -51 \\ \hline 33 \end{array}$$

$$\begin{array}{r} 21 \\ x - 4 \\ \hline -84 \end{array}$$

$$\frac{44z = 33}{44 \quad 44}$$

$$z = \frac{33}{44} = \frac{3}{4}$$

Now go back to
(1), (2) or (3) to substitute
 $y+z$ and solve for x!

$$(3) \quad -3x + y - 20z = -31$$

$$-3x - 4 - 20\left(\frac{3}{4}\right) = -31$$

$$-3x - \frac{16}{4} - \frac{60}{4} = -31$$

$$-3x - \frac{76}{4} = -31$$

$$-3x - 19 = -31$$

$$+19 \quad +19$$

$$\frac{-3x}{-3} = \frac{-12}{-3}$$

$$x = +4$$

$$(4, -4, \frac{3}{4})$$

$$4 \overline{) 736} \begin{array}{r} 19 \\ \underline{76} \\ 36 \end{array}$$

Lesson 4: 2/4

Exponent Rules:

$$x^m = \underbrace{x \cdot x \cdot x \cdots x}_{m\text{-times}}$$

$$x^{-m} = \frac{1}{x^m}$$

Ex $\frac{1}{x^2} = x^{-2}$

Rules:

$$\left(\frac{x}{y}\right)^m = \frac{x^m}{y^m}$$
$$x^m \cdot x^n = x^{m+n}$$
$$\frac{x^m}{x^n} = x^{m-n}$$

you can move powers "up" and "down" but must flip the sign of the exponent

Must have same base!

so $x^m \cdot y^n \neq x^{m+n}$
not allowed

$$(x^m)^n = x^{m \cdot n}$$

$$\frac{x^m}{x^n} = x^m \cdot x^{-n} = x^{m-n}$$

Ex a) $2^3 = 2 \cdot 2 \cdot 2 = 8$

b) $\left(\frac{1}{4}\right)^4 = \frac{1^4}{4^4} = \frac{1}{4 \cdot 4 \cdot 4 \cdot 4} = \frac{1}{256}$

$$\begin{array}{r} 3 \ 16 \\ \underline{16} \\ 96 \\ \underline{60} \\ 256 \end{array}$$

c) $4 \cdot 3^2 = 4 \cdot 9 = 36$

d) $x^2 \cdot x^3 = x^5$

e) $(-5)^7 \cdot (-5)^8 = (-5)^{15}$

f) $(-a^7 b^4)(3ab^9) \rightarrow$ multiply in any order we like
 $= (-1 \cdot 3)(a^7 \cdot a^1)(b^4 \cdot b^9)$
 $= \boxed{-3a^8 b^{13}}$

g) $\frac{2x^5 y^2}{xy} = 2 \cdot \frac{x^5}{x} \cdot \frac{y^2}{y} = 2x^4 y$

$$\begin{aligned} \text{ii) } \left(\frac{3xy^5}{6x^4} \right)^3 &= \frac{(3xy^5)^3}{(6x^4)^3} = \frac{3^3 x^3 y^{15}}{6^3 x^{12}} \\ &= \frac{1 y^{15}}{8 x^9} = \boxed{\frac{1}{8} \cdot x^{-9} y^{15}} \end{aligned}$$