Exam 4 Review

Math 1175, Fundamentals of Mathematics, Fall 2011, Mathematics and The Brooklyn Bridge

- 1. Explain why dividing both sides of $x^2 = 4x$ by x is an illegal operation. Hint: when solving equations, doing something which may eliminate a legitimate solution is not allowed.
- 2. In contrast to eliminating a legitimate solution, doing something that introduces an extraneous or false solution is allowed. Give an example of such a process and explain how, in spite of the introduction of false solutions, you can finish with the correct solution set.
- 3. You have now learned 3 methods for solving quadratic equations. What are they? Select your 2 favorite methods. Compare the advantages and disadvantages of the 2 you have selected. For each of your 2 selected methods, give an example of an equation best solved by that method.
- 4. Simplify a) $\sqrt{49x^{10}}$ b) $2p\sqrt{63p^5}$ c) $-3pq^2\sqrt{125k^7q^8}$
- 5. Simplify and multiply:

a)
$$(2\sqrt{3} - \sqrt{5})^2$$
 b) $3\sqrt{3}(\sqrt{2x} - 4x\sqrt{15})$ c) $(3\sqrt{2} + 2\sqrt{3})(2\sqrt{50} - 3\sqrt{12})$

6. Simplify and rationalize the denominator:

a)
$$\frac{\sqrt{24x^5}}{\sqrt{3x^2y}}$$
 b) $\frac{\sqrt{4x}}{2\sqrt{3}}$ c) $\frac{\sqrt{24}}{3-\sqrt{3}}$ d) $\frac{2\sqrt{3}-3\sqrt{2}}{\sqrt{3}+\sqrt{8}}$ e) $\frac{x\sqrt{2}}{x\sqrt{2}+3\sqrt{5}}$

7. Solve for *x* and check for extraneous solutions: $\sqrt{2}$

a)
$$x - \sqrt{x - 2} = 4$$

8. Use the square root property to solve for y:
b) $x = 4 + 3\sqrt{x - 4}$
c) $\sqrt{5 - x - x} = 1$

a)
$$y^2 = 135$$
 b) $(y+4)^2 = 169$

9. Solve for x using the quadratic formula. Express the answers in simplest radical form.

a)
$$x^2 + 10x + 7 = 0$$
 b) $3x^2 + 3 = 8x$ c) $x^2 - 6x = 4$ d) $(x+2)(x+4) = 2$

10. In $\triangle ABC$, $\angle C = 90^\circ$, AC = x - 1, BC = 2x, AB = 2x + 1. Find: a) x b) all three sides of $\triangle ABC$

c) area of $\triangle ABC$







12. Find exact and approximate perimeter of triangle to one decimal place





- 13. The rectangle has perimeter $12\sqrt{7}$ cm.
 - a) Find the exact value of *x*.
 - b) Find the area and perimeter of the rectangle.
- 14. One of the main cables of a model bridge has as equation $x^2 = 16h$ where x is the horizontal distance from its lowest point and h is the height above its lowest point. The span between the towers is 16 inches.
- a) Draw a sketch and determine the vertical height of the cable. (Hint: let x = 8, solve for h.)
- b) Determine exact and approx. location(s) where h is 2 inches. Use the square root principle in the solution.