

(1 point) CUNY/CityTech/CollegeAlgebra_Trig/NonLinearSystems/circle-hyperbola.pg
Solve the following system of equations.

$$3x^2 - 2y^2 = 1$$

$$3x^2 + 2y^2 = 5$$

Solution(s):

- Enter your answers as points: (x, y)
- Because these systems are non-linear, you may have more than one solution.
- If you have more than one solution, enter your answers as a list of points: (x₀, y₀), (x₁, y₁)
- Use 'sqrt(...)' to enter radical answers, do not use decimal approximations.

[Hint:](#)

[Solution:](#)

Elimination Method

$$3x^2 - 2y^2 = 1$$

$$3x^2 + 2y^2 = 5$$

$$\begin{array}{r} 6x^2 \qquad \qquad = 6 \\ x^2 \qquad \qquad = 1 \\ x \qquad \qquad = \pm 1 \end{array}$$

Pick one equation, substitute

$$\text{Let } x = -1$$

$$y = \pm 1$$

$$3x^2 + 2y^2 = 5$$

$$3(-1)^2 + 2y^2 = 5$$

$$3(1) + 2y^2 = 5$$

$$3 + 2y^2 = 5$$

$$\begin{array}{r} -3 \qquad \qquad \qquad -3 \\ \hline \end{array}$$

$$2y^2 = 2$$

$$y^2 = 1$$

→ (-1, -1), (-1, 1)
are solutions.

$$\text{Let } x=1$$

$$3x^2 + 2y^2 = 5$$

$$3(1)^2 + 2y^2 = 5$$

$$3(1) + 2y^2 = 5$$

$$3 + 2y^2 = 5$$

$$2y^2 = 2$$

$$y^2 = 1$$

$$y = \pm 1$$

$\rightarrow (1, -1), (1, 1)$
are solutions

o o Solutions

$$(x, y) \in \{(1, -1), (-1, 1), (1, -1), (1, 1)\}$$

Four total solutions!