

Ben Yusuf RIC question 4

Find the current in the RIC circuit, assuming that $E(t) = 0$ for $t > 0$.

4. $R = 6 \Omega$ $L = .1 \text{ henrys}$ $C = .004 \text{ farads}$ $Q_0 = 2 \text{ coulombs}$ $I_0 = -10 \text{ amperes}$.

To find the current in the RIC circuit, we need to solve second order equation that describes the circuit, For series RIC circuit with a resistor (R), inductor (L) and capacitor (C)

second order diff equation homogeneous $\Rightarrow \frac{1}{10} Q'' + 6 Q' + 250 Q = 0$
(we don't want in fraction so we multiply) $\Rightarrow Q'' + 60 Q' + 2500 Q = 0$

$$\rightarrow r^2 + 60r + 2500 = 0$$

quadratic formula $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \rightarrow \frac{-60 \pm \sqrt{60^2 - 4(1)(2500)}}{2(1)}$

$$\begin{cases} r_1 = -30 + 40i \\ r_2 = -30 - 40i \end{cases}$$

> second order homogeneous
Constant coefficient - Complex

$$\rightarrow \frac{-60 \pm \sqrt{3600 - 10000}}{2}$$

$$\rightarrow \frac{-60 \pm \sqrt{-6400}}{2}$$

$$\rightarrow \frac{-60 \pm 80i}{2}$$

$$\rightarrow -30 \pm 40i$$

$$\begin{cases} r_1 = -30 + 40i \\ r_2 = -30 - 40i \end{cases}$$

$$Q = e^{-30t} (3 \cos 40t + B \sin 40t)$$

unknown function

since $Q_0 = 3$ $I = Q' = e^{-30t} ((40B - 90) \cos 40t - (30B + 120) \sin 40t)$

$$I_0 = -10 \Rightarrow \frac{40B - 90}{+90} = \frac{-10}{+90}$$

$$40B = 80$$

$$\boxed{B = 2}$$

now, $-30B - 120 = -180$

$$-30(2) - 120 = -180$$

$$-60 - 120 = -180 \quad \checkmark$$

$$\boxed{I = -10 e^{-30t} (\cos 40t + 18 \sin 40t)}$$