

$$\int u dv = uv - \int v du$$

$u = \text{function of } u(x)$   
 $dv = \text{variable } dv$   
 $v = \text{function of } v(x)$   
 $du = \text{variable } du$

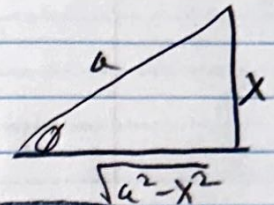
$$\frac{du}{1+u^2} = \arctan(u)$$

$$\sqrt{a^2 - x^2}$$

identity =  $1 - \sin^2 \theta = \cos^2 \theta$

$$x = a \sin \theta$$

$$\sqrt{a^2 - x^2} = a \cos \theta$$

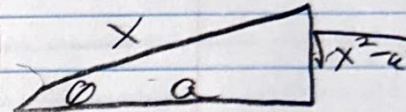


$$\sqrt{x^2 - a^2}$$

$$\sec^2 \theta - 1 = \tan^2 \theta$$

$$x = a \sec \theta$$

$$\sqrt{x^2 - a^2} = a \tan \theta$$

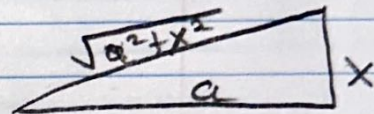


$$\sqrt{a^2 + x^2}$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$x = a \tan \theta$$

$$\sqrt{a^2 + x^2} = a \sec \theta$$



1) linear homogeneous

$$y' + p(x)y = 0 \rightarrow y = Ce^{-\int p(x) dx}$$

2) linear non-homogeneous

$$y' + p(x)y = f(x) \rightarrow \text{Step 1 - } y_1 \text{ if any solution of associated homog. eqn.}$$

$$\text{Step 2 - } y = u y_1$$

$$u' = \frac{f(x)}{y_1}$$

3) Separable  $h(y)y' = g(x)$  - Integrate both side w.r.t.  $x$

4) Bernoulli -  $y' + p(x)y = f(x)y^r \rightarrow \text{Step 1 - } y_1 \text{ is any solution of associated homog. eqn.}$

5) Non-linear homogeneous

$y' = f(x, y)$  where  $f(x, y)$  depends on  $y/x = u = g(u)$

$$\text{Step 2 - } y = u y_1$$

$$\frac{u'}{u^2} = f(x) y_1^{r-1}$$

$$\text{Step 1 - } y_1 = x, \text{ Step 2 - } y = u y_1 = ux, \frac{u'}{g(u)u} = \frac{1}{x}$$