

$\frac{dy}{dt} + p(t)y = g(t)$ is a(n) linear differential equation of order one with nonconstant (or variable)

coefficients. To solve the equation, we multiply both sides by $\mu(t) = \underline{e^{\int p(t)}}$, also known as

a(n) integral factor (2 words). The antiderivative of the LHS will then be $y\mu(t)$.

Thus, provided that the integral used to determine $\mu(t)$ can be found and that an antiderivative for $\mu(t)g(t)$ exists, then a closed form family of solutions can be found for the diffeq. Otherwise, the solution

will contain one or more unevaluated integral. Below you will find the family of solutions

$y = t^2 + \frac{c}{t^2}$ and the particular solution going through (1,2):

$y = t^2 + \frac{1}{t^2}$. The domain of this particular solution

is (0,∞). When $c=0$, we get the particular solution:

$y = t^2$ with domain (-∞,∞), which divides the family of solutions into those that are

asymptotic to the positive and negative y-axis.

