NYCCT MAT2572 Halleck Spring 2016 Practice exam 2

* You must use a graphing calculator.
* Actual exam will be about 1/3 of this practice exam in length.
* At the end of class, be sure to turn in your formula sheet (1 sheet, 2 pages, hand-written), worth 10%.
1. (10 pts) The formula **=$B$2\*C4** is located in cell D3.
	* 1. What does cell D3 evaluate to?
		2. If this was copied and pasted into cell **B1**, what would the resulting formula be?

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|  | **A** | **B** | **C** | **D** |
| **1** |  2 | ????????? | 4 |  5 |
| **2** | 3 | 3 | 8 | 6 |
| **3** | 5 | 4 | 3 | **=$B$2\*C4** |
| **4** | 4 | 3 | 4 | 9 |

1. (10 pts) Based on recent experience, 10-year-old passenger cars going through a motor vehicle inspection station have an 80% chance of passing the emissions test. Suppose that 200 such cars will be checked out next week. Find the number of cars that are expected to pass by
	1. using the definition of expectation.
	2. finding the expectation for ith car Xi and using
2. (15 pts) A typical day’s production of a certain electronic component is 12. The probability that one of these components needs rework is 0.11. Each component needing rework costs $100.
	1. What is the average daily cost for defective components?
	2. For the days when the production is exactly 12, find the standard deviation for the daily cost for the defective components.
3. (35 pts) Let.
	1. Find *a* so that fY (y) is a PDF.
	2. Graph fY (y) from 0 ≤ y ≤ 3 (plot every 0.5).
	3. Find and graph FY (y), the corresponding CDF, from 0 ≤ y ≤ 3 (plot every 0.5).
	4. Find. Graph the inequality on your plot from part b) and shade the area representing the probability.
	5. Find the expectation and label on your plot from part b)
	6. Find the median and label on both graphs (the first with a vertical line and the second with a horizontal line and a vertical line).
	7. Compare the relative positions of the median and the expectation. Explain how the comparison relates to any skewing.
4. (40 pts) Consider an experiment that consists of withdrawing a ball from the box, NOT replacing it, and withdrawing a second ball. There are 2 red and 4 green balls in the box.
	1. What is the sample space of this experiment? Is this a random variable? Why or why not?
	2. To get a random variable W, we count the number of red balls selected. Find the possible outcomes and express their probabilities as quotients of binomial coefficients.
	3. Evaluate the binomial coefficients, leaving as fractions. Write W as a matrix with row 1 as the outcomes and row 2 the corresponding probabilities.
	4. Use the 2 row matrix of c to find the expectation μ=E(W).
	5. Find the 2 row matrix for W2 and use it find μ2=E(W2).
	6. Use the results from d and e to find V(W).
	7. If X is an RV indicating whether the first ball is red or not (1, 0 respectively) and Y is whether the second ball is red or not (1, 0 respectively). Find E(X) and E(Y) and show that their sum corresponds to your answer in d.
	8. Find V(X) and V(Y) for X and Y described in f. and show that their sum DOES NOT correspond to your answer in d. Why not? Try to reason why it is more or less.
5. (25 pts) Two chips are drawn at random and without replacement from an urn that contains five chips, numbered 1 through 5. If the sum of the chips drawn is even, the random variable X = 5; if the sum of the chips drawn is odd, X = −3.
	1. Use a 5 x 5 grid with the diagonal filled in to find the possible sums of the chips. Circle those that are even and count them. Use the count to write X as a 2 x 2 matrix.
	2. Using the definition, find the moment-generating function for X.
	3. Write X as a linear function of a Bernoulli distribution.
	4. Use the table to find the MGF of this Bernoulli distribution.
	5. Use your results from b and c and a theorem to find the MGF of X.
6. (25 pts) Let Y be a uniform random variable defined over the interval (0, 2).
	1. Find a formula for the rth moment of Y about the origin.
	2. Use the formula of a. to find the first 4 moments.
	3. Use b. and binomial expansion to find σ2 = E[(Y −μ)2].
	4. Use b. and binomial expansion to find E[(Y −μ)4].
	5. Use c. and d. to find the Kurtosis γ2.
7. (20 pts) For the exponential pdf 
	1. Find the moment generating function MY(t) using the definition.
	2. Use MY(t) to find the first moment μ.
	3. Use MY(t) to find the second moment μ2 and the variance σ2.
	4. Use MY(t) to find the third moment μ3 and the skewing γ1.
8. (15 pts) Given the MGF :
	1. Use the table to identify the distribution.
	2. Use MY(t) to find the first moment μ.
	3. Use MY(t) to find the second moment μ2 and the variance σ2.
9. (10 pts) Given the MGF ?
	1. Use the table to identify the distribution.
	2. Use MY(t) to find the third moment μ3.
10. (40 pts) Use Theorem 3.12.3 and the table to determine which of the following statements is true. If the statement is not true, then use the table to identify the distribution.
11. The sum of two independent exponential random variables with the same parameter λ has an exponential distribution.
12. The sum of two independent binomial random variables with the same parameter *p* has a binomial distribution.
13. The sum of two independent geometric random variables with the same parameter *p* has a geometric distribution.
14. The sum of two independent normal random variables has a normal distribution.

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| **Distribution** | ***fY*(*y*)** | ***MX*(*t*)** |
| Binomial B(n, p) |  |  |
| Geometric (counting failures only) |  |  |
| Negative Binomial(counting failures) |  |  |
| Poisson |  |  |
| Uniform |  |  |
| Uniform discrete |  |  |
| Normal |  |  |
| Exponential |  |  |
| Gamma |  |  |