

## Induced charge on a grounded conducting sphere

A point charge  $q$  is placed at a distance  $\vec{y}$  from the center of a grounded conducting sphere of radius  $a$ . The induced surface charge density is

$$\sigma(\gamma) = -\frac{q}{4\pi a y} \frac{1 - \frac{a^2}{y^2}}{\left(1 + \frac{a^2}{y^2} - 2\frac{a}{y} \cos \gamma\right)^{\frac{3}{2}}},$$

where  $\gamma$  is the angle between the line going from the center of the sphere to the charge  $q$  and the line going from the center of the sphere to the point on the surface of the sphere where the surface charge density is  $\sigma$ .

Calculate the total charge on the surface of the sphere.

