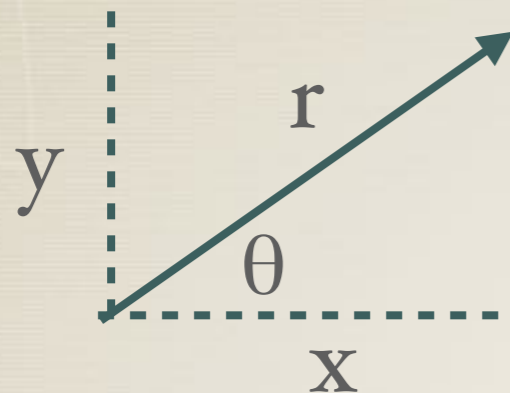


# PHYS 1441

## Review 2

# Vectors



$$x = r \cos(\theta)$$

$$y = r \sin(\theta)$$

$$r = \sqrt{x^2 + y^2}$$

$$\theta = \arctan \frac{y}{x}$$

components are independent  
and can be treated like scalars

# Kinematics

$$\vec{v} = \frac{d\vec{r}}{dt} \qquad \vec{a} = \frac{d\vec{v}}{dt}$$

if  $a$  is constant:

$$x = x_0 + v_{x0}t + \frac{1}{2}a_x t^2$$

$$v_x = v_{x0} + a_x t$$

$$v_x^2 = v_{x0}^2 + 2a_x(x - x_0)$$

# Angular Kinematics

$$\omega = \frac{d\theta}{dt}$$

$$\alpha = \frac{d\omega}{dt}$$

$$L = R\theta$$

$$v = R\omega$$

$$a_{tan} = R\alpha$$

$$a_R = -\frac{v^2}{R}$$

if  $\alpha$  is constant:

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

$$\omega = \omega_0 + \alpha t$$

$$\omega^2 = \omega_0^2 + \alpha(\theta - \theta_0)$$

# Forces and Torques

$$\vec{F} = m\vec{a}$$

$$\vec{F}_{ab} = -\vec{F}_{ba}$$

$$\vec{F}_g = mg$$

$\vec{F}_N =$  what it needs to be  
to keep the object  
from going through  
the surface

$$\tau = RF \sin \theta$$

$$\tau = I\alpha$$

$$F_{fr} = \mu F_N$$

$$F_G = G \frac{M_1 M_2}{R^2}$$

$$F_s = -kx$$

# Energy

Is conserved if only conservative forces

$$W = \int \vec{F} \cdot d\vec{x} \quad \text{if } F \text{ is constant} \quad W = \vec{F} \cdot \vec{x}$$

$$KE = \frac{1}{2}mv^2 \quad KE = \frac{1}{2}I\omega^2$$

$$U(x) = \int F(x)dx$$

$$U_g(h) = mgh \quad U_s(x) = \frac{1}{2}kx^2 \quad U_G(r) = -G\frac{M_1M_2}{R}$$

$$\text{Power } P = \frac{dE}{dt} = \vec{F} \cdot \vec{v} \quad \text{if } F \text{ is constant}$$

# Momentum

Is conserved if no outside force (torque)

$$\vec{p} = m\vec{v}$$

$$L = I\omega = mvR \sin \theta$$

$$\vec{F} = \frac{d\vec{p}}{dt}$$

$$\tau = \frac{dL}{dt}$$

example: collision that stick together

$$m_A v_A + m_B v_B = (m_A + m_B) v'$$

# Statics

$$\sum F = 0$$

$$\sum \tau = 0$$