

Review Sheet for Test #2

Compute the difference quotient $\frac{f(x+h)-f(x)}{h}$ for the functions.

1) $f(x) = x^2 - 3x + 7$

2) $f(x) = x^2 + 2x - 10$

For the given function and corresponding root, find the value of C, find the **exact** values of the remaining roots of the function, and draw a sketch of the function, labeling the roots.

3) $f(x) = 2x^3 - 4x^2 - 33x + C$, root $x = 5$

4) $f(x) = x^3 + 11x^2 + 32x + C$, root $x = 4$

Solve the equation and round to the nearest thousandth.

5) $7\log_4(x) = 12$

6) $10e^{19-7x} = 85$

Solve the inequality and express your answer in interval notation.

7) $\frac{x+5}{x-3} \geq 0$

8) $\frac{2x+10}{x-7} < 0$

9) $|4x - 3| > 25$

10) $|2x + 10| \leq 14$

Evaluate to the nearest hundredth:

11) $\log_{9.2}(2545.7)$

12) $\log_5(1000)$

Use algebra to find the inverse of the given function

13) $h(x) = \frac{7}{2x+5}$

14) $g(x) = \frac{x+2}{x-6}$

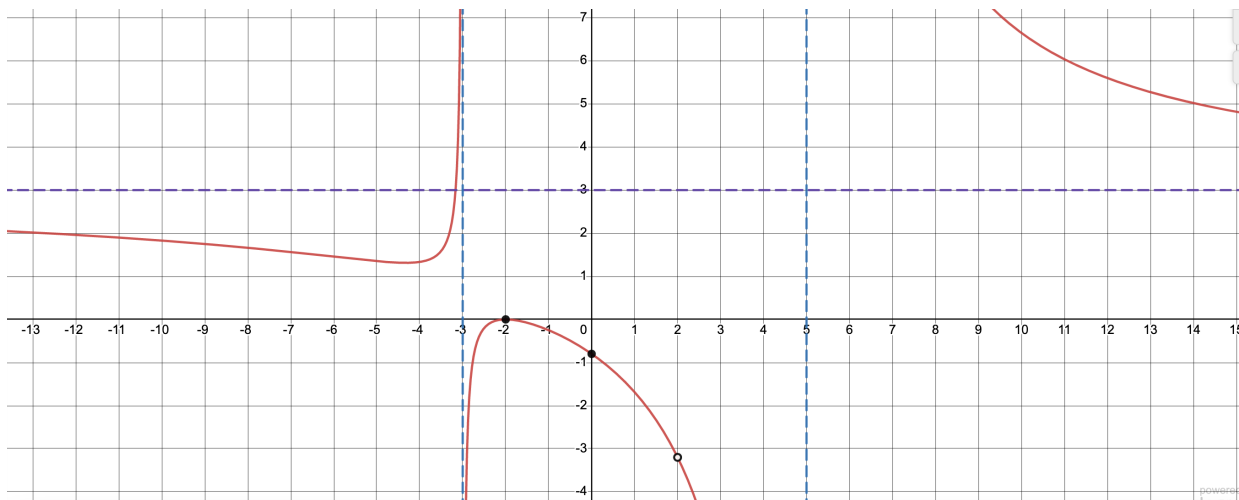
15) If $f(x) = \sqrt{10 - 2x}$, and $g(x) = x + 2$, find

a) $(f \circ g)(x)$

b) $(f \circ g)(-9)$

c) Domain of $\frac{f(x)}{g(x)}$

16) For $f(x)$, below, find:



a) Domain

b) Vertical & Horizontal Asymptote(s)

c) x and y intercept(s)

d) Hole(s)

e) Write the function

17) An organism contains 3,259 bacteria and growing at a rate of 7.5% per day.

a) How many bacteria will the organism contain after 15 days?

b) How long will it take for the bacteria to double?

Expand the logarithm

18) $\text{Log} \left(\frac{x^9 z^7}{y^{15}} \right)$

19) $\text{Log} \left(\sqrt{\frac{x^{10}}{y^5}} \right)$

- 20) Find the domain, asymptotes, and x-intercepts of the function $f(x) = \text{Log}(x - 3)$, and then sketch its graph.
- 21) Give an expression for $f(x)$, with leading coefficient 2, of degree 3, having roots of $x = 1$, and $x = 1 + 2i$. You may leave your answer in factored form but without imaginary coefficients.
- 22) Give an expression for $f(x)$ with roots of $x = -2, 6$, and 1 with multiplicity 4. $f(x)$ must also intersect $(-3, -9216)$.

Find the **exact** value of

23) $\tan\left(-\frac{11\pi}{6}\right)$

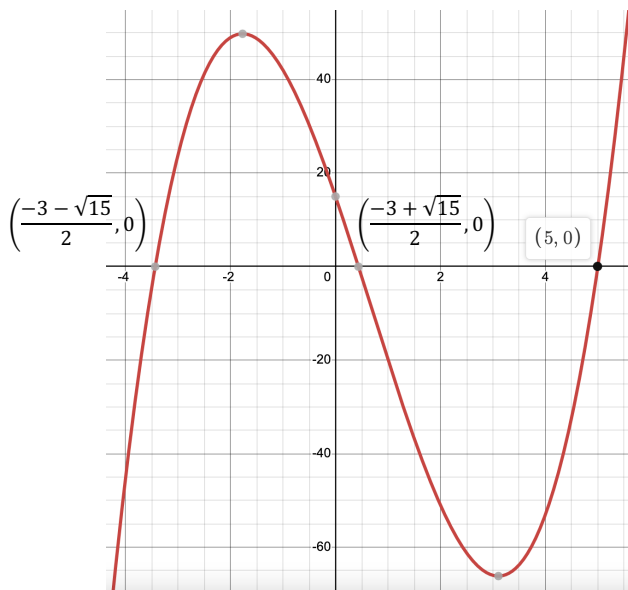
24) $\sec\left(-\frac{3\pi}{4}\right)$

Answer Key

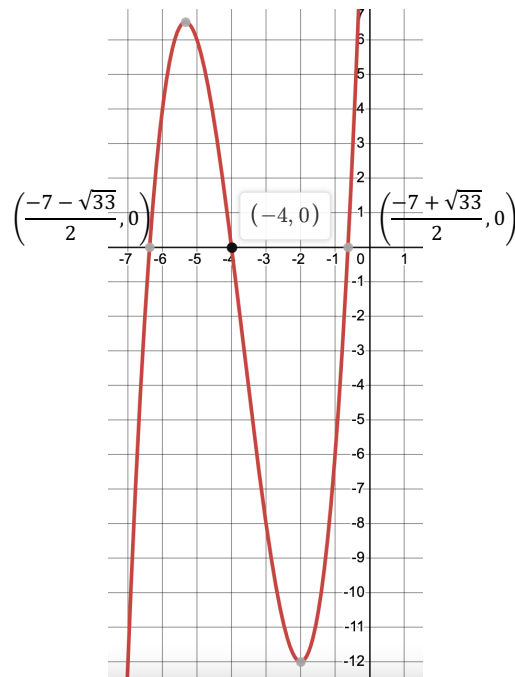
1) $2x + h - 3$

2) $2x + h - 2$

3) $C = 15$, Roots: $5, \frac{-3 \pm \sqrt{15}}{2}$



4) $C = 16$, Roots: $4, \frac{-7 \pm \sqrt{33}}{2}$



5) $x = 4^{\frac{12}{7}} = 10.767$

6) $x = 2.409$

7) $(-\infty, -5] (3, \infty)$

8) $(-5, 7)$

9) $\left(-\infty, -\frac{11}{2}\right) (7, \infty)$

10) $[-12, 2]$

11) 3.534

12) 4.292

13) $h^{-1}(x) = \frac{7-5x}{2x}$

14) $g^{-1}(x) = \frac{6x+2}{x-1}$

15) a) $\sqrt{6-2x}$ b) $2\sqrt{6}$ c) $(-\infty, -2) (-2, 5]$

16) a) $(-\infty, -3)(-3, 5)(5, \infty)$ b) VA: $x = 5, x = -3$, HA: $y = 3$

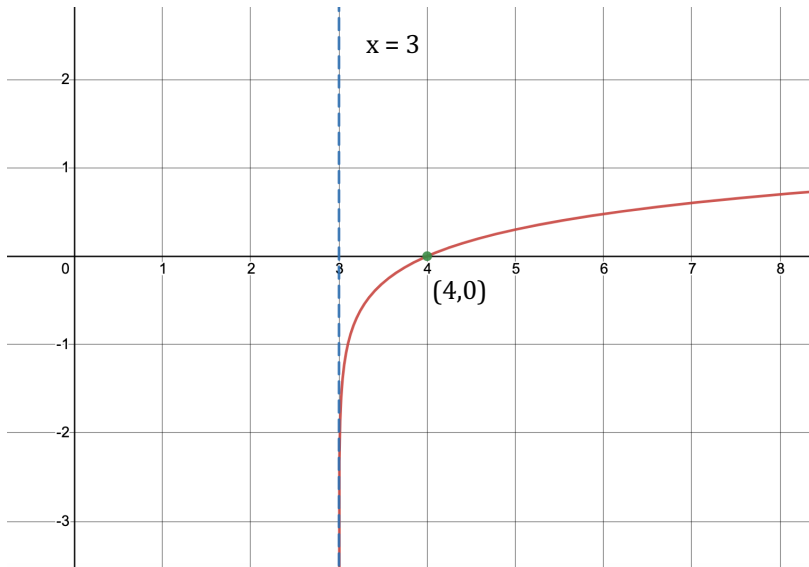
c) x-int: $(-2, 0)$ y-int: $(0, -\frac{4}{5})$ d) $(2, -\frac{16}{5})$ e) $f(x) = \frac{3(x+2)^2(x-2)}{(x-2)(x-5)(x+3)}$

17) a) 9643 bacteria b) 9.584 days

18) $9\text{Log}(x) - 15\text{Log}(y) + 7\text{Log}(z)$

19) $5\text{Log}(x) - \frac{5}{2}\text{Log}(y)$

20) a) D: $(3, \infty)$ VA: $x=3$ x-int: $(4, 0)$



21) $f(x) = 2(x-1)(x^2 - 2x + 5)$

22) $f(x) = -4(x+2)(x-6)(x-1)^4$

23) $\frac{\sqrt{3}}{3}$

24) $-\sqrt{2}$