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Linear Algebra pg 47 #1-21 odd

**Determine if the system has a nontrivial solution.**

$$1. \begin{bmatrix} 2 & -5 & 8 & 0 \\ -2 & -7 & 1 & 0 \\ 4 & 2 & 7 & 0 \end{bmatrix} \sim \begin{bmatrix} 2 & -5 & 8 & 0 \\ 0 & -12 & 9 & 0 \\ 0 & 12 & -9 & 0 \end{bmatrix} \sim \begin{bmatrix} 2 & -5 & 8 & 0 \\ 0 & -12 & 9 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Yes, this system has nontrivial solutions for each value of  $X_3$  since  $X_3$  is a free variable.

$$3. \begin{bmatrix} -3 & 4 & -8 & 0 \\ -2 & 5 & 4 & 0 \end{bmatrix} \sim \begin{bmatrix} -3 & 4 & -8 & 0 \\ 0 & 7/3 & 2/3 & 0 \end{bmatrix}$$

Yes, this system has nontrivial solutions for each value of  $X_3$  since  $X_3$  is a free variable.

**Write the solution set of the given homogeneous system in parametric vector form.**

$$5. \begin{aligned} 2x_1 + 2x_2 + 4x_3 &= 0 \\ -4x_1 - 4x_2 - 8x_3 &= 0 \\ -3x_2 - 3x_3 &= 0 \end{aligned}$$

$$\begin{bmatrix} 2 & 2 & 4 & 0 \\ -4 & -4 & -8 & 0 \\ 0 & -3 & -3 & 0 \end{bmatrix} \sim \begin{bmatrix} 2 & 2 & 4 & 0 \\ 0 & -3 & -3 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}, \quad x = \begin{matrix} x_1 \\ x_2 \\ x_3 \end{matrix} = \begin{matrix} 1 \\ -1 \\ 0 \end{matrix}$$

**Describe all solutions of  $Ax = 0$  in parametric vector form, where  $A$  is row equivalent to the given matrix.**

$$7. \begin{bmatrix} 1 & 3 & -3 & 7 \\ 0 & 1 & -4 & 5 \end{bmatrix}$$

$$X = \begin{matrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{matrix} = x_3 \begin{matrix} -9 \\ 4 \\ 1 \\ 0 \end{matrix} + x_4 \begin{matrix} 8 \\ -5 \\ 0 \\ 1 \end{matrix}$$

$$9. \begin{bmatrix} 3 & -6 & 6 \\ -2 & 4 & -2 \end{bmatrix} \sim \begin{bmatrix} 1 & -2 & 4 \\ -2 & 4 & -2 \end{bmatrix} \sim \begin{bmatrix} 1 & -2 & 4 \\ 0 & 0 & 6 \end{bmatrix} \quad X = \begin{matrix} x_2 \\ x_3 \end{matrix} \begin{matrix} 2 \\ 1 \\ 0 \end{matrix}$$

11. I couldn't figure out how to make a matrix that big with so many entries, but the variables that is free are  $x_2$ ,  $x_4$ ,  $x_6$ . The basic variables are  $x_1$ ,  $x_3$ , and  $x_5$

**13. Suppose the solution set of a certain system of linear equations can be described as  $x_1 = 5 + 4x_3$ ,  $x_2 = -2 - 7x_3$ , with  $x_3$  free. Use vectors to describe this set as a line in  $R^3$**

I don't understand this question.

**15. Describe and compare the solution sets of  $x_1 + 5x_2 - 3x_3 = 0$  and  $x_1 + 5x_2 - 3x_3 = -2$ .**

From what I think I understood from page 46, theorem 6 if  $Ax = b$  has a solution, then the solution set is obtained by translating the solution set of  $Ax = 0$ ; meaning that the solution sets are parallel.

17. Follow the method of Example 3 to describe the solutions of the following system in parametric vector form.

$$\begin{aligned}2x_1 + 2x_2 + 4x_3 &= 8 \\ -4x_1 - 4x_2 - 8x_3 &= -16 \\ -3x_2 - 3x_3 &= 12\end{aligned}$$

$$\begin{bmatrix} 2 & 2 & 4 & 8 \\ -4 & -4 & -8 & -16 \\ 0 & -3 & -3 & 12 \end{bmatrix} \sim \begin{bmatrix} 2 & 2 & 4 & 8 \\ 0 & -3 & -3 & 12 \\ -4 & -4 & -8 & -16 \end{bmatrix} \sim \begin{bmatrix} 2 & 2 & 4 & 8 \\ 0 & -3 & -3 & 12 \\ 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} x_1 & 8 \\ x_2 & -4 \\ x_3 & 0 \end{matrix}$$

19. Find the parametric equation of the line through a parallel to b.

$$\mathbf{a} = \begin{bmatrix} -2 \\ 0 \end{bmatrix}, \quad \mathbf{b} = \begin{bmatrix} -5 \\ 3 \end{bmatrix} \quad \mathbf{x} = \mathbf{a} + by \quad y \text{ is the boundary}$$

21. Find a parametric equation of the line M through p and q.

$$\mathbf{p} = \begin{bmatrix} 3 \\ -3 \end{bmatrix}, \quad \mathbf{q} = \begin{bmatrix} 4 \\ 1 \end{bmatrix} \quad \mathbf{x} = \mathbf{p} + y(\mathbf{q} - \mathbf{p})$$