

Check by differentiation that  $y = 5 \cos 2t + 4 \sin 2t$  is a solution to  $y'' + 4y = 0$  by finding the terms in the sum:

$$y'' = -5 \cos 2t - 4 \sin 2t$$

$$4y = 5 \cos 2t + 4 \sin 2t$$

$$\text{So } y'' + 4y = 0$$

Solution:

check  $y = 5 \cos 2t + 4 \sin 2t$

is soln  $y'' + 4y = 0$

$$y' = 5(-\sin 2t \cdot 2) + 4 \cos 2t \cdot 2$$

$$y' = -10 \sin 2t + 8 \cos 2t$$

$$y'' = -20 \cos 2t - 16 \sin 2t$$

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$$4y = 20 \cos 2t + 16 \sin 2t$$

derivative of  
 $\frac{d}{dt} \sin t = \cos t$

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$$f(x) = \underline{\hspace{2cm}}$$

$$\underline{\underline{f(1) = -2}}$$

$$\underline{\underline{f'(x) = 20x^3 + 12x + 8}}$$

$$\text{ans: } f(x) = 5x^4 + 6x^2 + 8x \leftarrow$$

$$f(x) = 5x^4 + 6x^2 + 8x + 7 \leftarrow$$

$$f(x) = 5x^4 + 6x^2 + 8x + 123 \leftarrow$$

$$f(x) = 5x^4 + 6x^2 + 8x + C$$

sub  $x=1, f(x)=-2$

$$-2 = 5 \cdot 1^4 + 6 \cdot 1^2 + 8 \cdot 1 + C$$

$$-2 = 19 + C$$

$$\boxed{-21 = C}$$

$$\boxed{f(x) = 5x^4 + 6x^2 + 8x - 21}$$

Consider the function  $f(x) = x^4 + 2\sqrt{x}$ .

Let  $F(x)$  be the antiderivative of  $f(x)$  with  $F(1) = -2$ .

Then  $F(x) =$

**Solution:**

Goal: find  $F(x)$   
Deriv. of  $F(x)$  →  $f(x)$  is antideriv. of  $f(x)$   
 $F(1) = -2$

$$\boxed{f(x) = x^4 + 2\sqrt{x}}$$

$F(x)$

Inverse Goal: find  $f(x)$   
find  $f(x)$  where  
 $f'(x) = x^4 + 2\sqrt{x} \leftarrow$   
and  $f(1) = -2 \leftarrow$

$f(x)$

$F'(x)$

deriv.  $f(x)$

deriv.  $f'(x)$

## Results for this submission

### Answer Preview

$$\frac{7x^{-1}}{-1} + 2\ln(x) - 8x + 17$$

The answer above is NOT correct.

Find the particular antiderivative that satisfies the following conditions:

$$\frac{dy}{dx} = 7x^{-2} + 2x^{-1} - 8; \quad y(1) = 4.$$

$$y = \frac{7x^{-1}}{-1} + 2\ln(x) - 8x + 19$$

$$\frac{dy}{dx} = 7x^{-2} + 2x^{-1} - 8$$

check: does  $y(1) = 4$ ?

plug in  $x=1$ , see if  $y=4$ .

$$y = \frac{7x^{-1}}{-1} + 2\ln - 8x + 19$$

⊗ practice for Calc II