

# Intro

Goal: find the unknown function  $y$ ,  $f$   
 $f(x)$ ,  $f(t)$

typical answer:

$$y = 3x^2 + 6$$

$$f(x) = \sin x \cdot e^x$$

What if the derivative is:

Hint

$$y' = x^3$$

Integrate:

$$\int y' dx = \int x^3 dx$$

$$y = \frac{1}{4}x^4$$

an example of a differential eq.

this is not the function I was thinking of.

Hint:

$$y(1) = 2$$

plug in 1 for  $x$ , get  $y = 2$ .

$$y = \frac{1}{4}x^4$$

plug in:

$$y = \frac{1}{4} \cdot 1^4 = \frac{1}{4}$$

$$y(1) = \frac{1}{4} \quad \text{Doesn't work}$$

$$y = \frac{1}{4}x^4 + C$$

examples of antiderivatives of  $x^3$ :

$$y = \frac{1}{4}x^3 + 2$$

satisfies  $y' = x^3$

$$y = \frac{1}{4}x^3 - 11$$

satisfies  $y' = x^3$

which value of  $C$  gives  $y(1) = 2$ ?

plug in  $y(1) = 2$

$$2 = \frac{1}{4}1^4 + C$$

$$2 - \frac{1}{4} = C$$

$$2 - \frac{1}{4} + C$$
$$-\frac{1}{4} - \frac{1}{4}$$

$$\frac{5}{4} \cdot 2 - \frac{1}{4} = C$$

$$\frac{8}{4} - \frac{1}{4} = C$$

$$\frac{7}{4} = C$$

The unknown function

is

$$y = \frac{1}{4}x^4 + \frac{7}{4}$$

Ex 2 Find  $y$ .

if

$$y = \frac{x}{2} \cdot y'$$

diff.  
eq.

Goal: Find  $y = \underline{\quad?}$   
that makes the  
equation true.

How do we do  
this?

NO IDEA ←

Where did this  
come from?

Is  $y = x^2$  a solution  
to this diff. eq.

find  $y' = 2x$

plug in  $y = x^2, y' = 2x$

into  $y = \frac{x}{2} \cdot y'$

$$x^2 = \frac{x}{2} \cdot 2x$$

$$x^2 = x^2 \checkmark$$

Yes,  $y = x^2$  is  
a solution.